

Nevio Benvenuto

Giovanni Cherubini

Algorithms for Communications Systems and their Applications

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To Adriana, and to Antonio, Claudia, and Mariuccia

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